

## Acceleration + Displacement

Displacement  $\Rightarrow$  area under  $v-t$  graph

Constant Velocity:  $v = \frac{\Delta d}{\Delta t}$

Constant Acceleration:

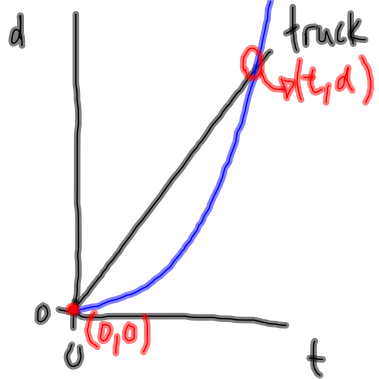
$v_{ave} = \frac{\Delta d}{\Delta t}$  and  $a = \frac{\Delta v}{\Delta t}$

*Handwritten notes:*  
 $v_{ave} = \frac{v_1 + v_2}{2}$  (with arrow pointing to  $v_{ave}$ )  
 $v_2 = v_1 + at$  (with arrow pointing to  $\Delta v$ )

maybe useful

$$\left\{ \begin{array}{l} \Delta d = v_1 t + \frac{1}{2} a t^2 \\ \Delta d = v_2 t - \frac{1}{2} a t^2 \\ v_2^2 = v_1^2 + 2 a \Delta d \end{array} \right.$$

MP187



Truck - constant velocity

$$v = \frac{\Delta d}{\Delta t}$$

$$v = \frac{d-0}{t-0}$$

$$v = \frac{d}{t}$$

$$22\text{m/s} = \frac{d}{t}$$

$$d = (22\text{m/s})t$$

Car - constant acc.

$$v_i = 0$$

$$a = 4.8\text{m/s}^2$$

$$\Delta d = ?$$

$$\Delta t = ?$$

$$\Delta d = v_i t + \frac{1}{2} a (\Delta t)^2$$

$$d = 0(t) + \frac{1}{2} (4.8\text{m/s}^2) t^2$$

$$d = (2.4\text{m/s}^2) t^2$$

$$(22\text{m/s})t = (2.4\text{m/s}^2)t^2$$

$$0 = 2.4t^2 - 22t$$

$$0 = t(2.4t - 22)$$

$$t = 0 \quad \text{and} \quad 2.4t - 22 = 0$$

$$2.4t = 22$$

$$t = \frac{22\text{m/s}}{2.4\text{m/s}^2}$$

$$t = 9.2\text{s}$$

$$\begin{aligned} \frac{\text{m/s}}{\text{m/s}^2} &= \frac{\text{m}}{\text{s}} \div \frac{\text{m}}{\text{s}^2} \\ &= \frac{\cancel{\text{m}}}{\text{s}} \times \frac{\text{s}^2}{\cancel{\text{m}}} \\ &= \text{s} \end{aligned}$$

It will take 9.2s for the car to catch up with the truck

Example

An airplane must reach a velocity of  $71 \text{ m/s}$  for takeoff.

If the runway is  $1.0 \text{ km}$  long, what must the acceleration be?

$$\begin{aligned}
 v_1 &= 0 \\
 v_2 &= 71 \text{ m/s} \\
 \Delta d &= 1.0 \text{ km} = 1.0 \times 10^3 \text{ m} \\
 a &= ??
 \end{aligned}$$

$$\begin{aligned}
 v_2^2 &= v_1^2 + 2a\Delta d \\
 v_2^2 - v_1^2 &= 2a\Delta d \\
 a &= \frac{(v_2^2 - v_1^2)}{(2\Delta d)} \\
 a &= \frac{(71 \text{ m/s})^2 - 0^2}{2(1.0 \times 10^3 \text{ m})}
 \end{aligned}$$

$$a = 2.5 \text{ m/s}^2$$

To Do:

① PP/89

② Calculator Pad / kinematics  
1-15